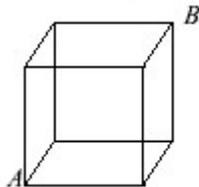


1. Each edge of a cubic water container is  $2\text{ m}$  long.  
 What is the volume of the cube (in  $\text{m}^3$ )? \_\_\_\_\_ ( $\text{m}^3$ ) 1
2. A jar contains 7 marbles: 2 white, 2 yellow, and 3 black. You removed one marble at random. What is the probability that you removed a yellow marble? Express your answer as a fraction in lowest terms. \_\_\_\_\_ 2

3. Simplify to a fraction in lowest terms:  $\frac{4/30}{2/10}$  \_\_\_\_\_ 3

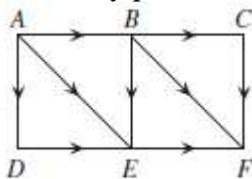
4. How many minutes are there in 5 hours? \_\_\_\_\_ (min) 4
5. The edges of the wooden cube (below) are  $15\text{ cm}$  each. An ant walks the shortest possible distance along the edges of the cube starting at corner  $A$  and ending at corner  $B$ . What distance does the ant have to travel (in  $\text{cm}$ )?



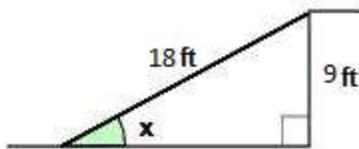
\_\_\_\_\_ ( $\text{cm}$ ) 5

6. The average of 2 numbers is 2013. What is their sum? \_\_\_\_\_ 6

7. Valid paths are along the lines in directions specified by arrows.  
 How many paths are there from  $A$  to  $F$ ?



8. What is the value (in degrees) of the angle marked by the letter  $x$ ? \_\_\_\_\_ 7



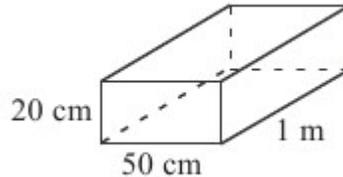
\_\_\_\_\_ ( $^\circ$ ) 8

9. Round  $\sqrt{255}$  to the nearest whole number. \_\_\_\_\_ 9

Grade Five (5) Division

10. You bought one pencil for \$0.49, one eraser for \$0.59, and 2 pens for \$0.75 each. How much money did you spend in total (in dollars correct to 2 decimal places)? \_\_\_\_\_ (\$) 10

11. What is the volume of the box below (in  $m^3$ )? Express your answer as a



decimal correct to 1 decimal place. \_\_\_\_\_ ( $m^3$ ) 11

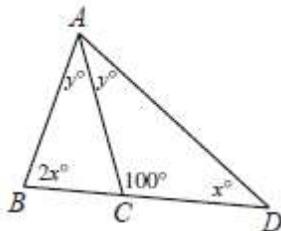
12. 75% of the 36 boys in the hiking club and 87.5% of the 64 girls in the hiking club participated in the yearly field trip.

What percentage of the school hiking club participated in the field trip? \_\_\_\_\_ (%) 12

13. Andrew, Betty, and Carla together spent N dollars, of which one third was spent by Andrew, one fourth was spent by Betty, and 10 dollars were spent by Carla. How many dollars did Andrew spend? \_\_\_\_\_ (\$) 13

14. A survey of 100 households showed that the average number of cars per household was 1.5. If 40 of the households did not have any car, what was the average number of cars among the households that had at least one car? Give the answer as a decimal, to the nearest tenth. \_\_\_\_\_ 14

15.  $x$  and  $y$  are measures of angles in  $\triangle ABC$  and  $\triangle ACD$  as shown below (the figure is not drawn to scale). What is the value of  $x$  (in degrees)?



\_\_\_\_\_ (°) 15

16. The binary representation of any non-negative integer is as follows: 0 (for the number 0), 1 (for 1), 10 (for 2), 11 (for 3), 100 (for 4), and so on. What number has the binary representation 100111? \_\_\_\_\_ 16

17. In the  $4 \times 4$  grid below, every grid point is 1 unit from its nearest horizontal or vertical neighbours. How many lines pass through exactly 2 grid points?



\_\_\_\_\_ 17

18. Note that  $2 + 4 + 6 + \dots + 16 + 18 + 20 = 110$ . What is the value of  $1 + 2 + 3 + \dots + 8 + 9 + 10$ ? \_\_\_\_\_ 18

Grade Five (5) Division

19. How many positive integers smaller than 2013 are divisible both by 3 and 37? \_\_\_\_\_ 19

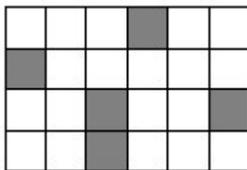
20. Alice made a list of all the positive prime numbers smaller than 100. How many times did she write the digit 5? \_\_\_\_\_ 20

21.  $a, b, c, d, e,$  and  $f$  are all different digits and none is 1 or 0. What is the positive difference between  $c$  and  $f$ ?

$$\begin{array}{r} \phantom{+} \phantom{+} \phantom{+} \phantom{+} \phantom{+} \\ \phantom{+} \phantom{+} \phantom{+} \phantom{+} \phantom{+} \\ + \phantom{+} \phantom{+} \phantom{+} \phantom{+} \phantom{+} \\ \hline 1 \phantom{0} \phantom{0} \phantom{0} \phantom{0} \end{array}$$

22. The entry fee per student to the Elmacon competition is \$20. The competition costs to PIMS are as follows: (a) \$11 per student for the competition material, food, and pencils; (b) \$2300 for prizes, mail, meetings, and operations; and (c) \$355 extra cost for the site if the number of students exceeds 250. How many students need to participate so that PIMS does not lose money? \_\_\_\_\_ 21

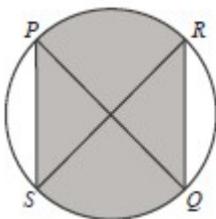
23. The figure below consists of a collection of black and white squares with area 1 each. How many rectangles with area 2 consist of exactly one white square and one black square? \_\_\_\_\_ 22



24. Let  $\Phi(a, b)$  be the mean of the numbers  $a$  and  $b$ . What is the value of  $\Phi(\Phi(\Phi(128,64),32),16)$ ? \_\_\_\_\_ 24

25. The taps of the swimming pool will fill it in 10 hours. If no water added, a full swimming pool will be drained completely in 12 hours. If the taps to fill the swimming pool are turned on but the drainage is not shut off, how many hours will it take for the swimming pool to fill up? \_\_\_\_\_ (hrs) 25

26.  $PQ \perp RS$  are both diameters of length 10 cm. What is the area of the shaded region rounded to the nearest whole number of  $cm^2$ ?



\_\_\_\_\_ ( $cm^2$ ) 26